# Learning Analytical Posterior Probability for Human Mesh Recovery 

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#### Abstract

Despite various probabilistic methods for modeling the uncertainty and ambiguity in human mesh recovery, their overall precision is limited because existing formulations for joint rotations are either not constrained to $\mathcal{S O}(3)$ or difficult to learn for neural networks. To address such an issue, we derive a novel analytical formulation for learning posterior probability distributions of human joint rotations conditioned on bone directions in a Bayesian manner, and based on this, we propose a new posterior-guided framework for human mesh recovery. We demonstrate that our framework is not only superior to existing SOTA baselines on multiple benchmarks but also flexible enough to seamlessly incorporate with additional sensors due to its Bayesian nature. The code is available at https:// github.com/NetEase-GameAI/ProPose.


## 1. Introduction

Human mesh recovery is a task of recovering body meshes and 3D joint rotations of human actors from images, which has ubiquitous applications in animation production, sports analysis, etc. To achieve this goal, various approaches have been proposed in the computer vision community. Existing methods can be divided into two categories, i.e., direct and indirect, respectively. Direct methods use neural networks to regress the rotations (e.g., axis angle [22], rotation matrix [34], 6D vector [29,37,74]) of each humanoid joint in an end-to-end way, while indirect methods recover joint rotations based on some intermediately predicted proxies (e.g., 3D human keypoints [19, 36, 42], 2D heatmaps [52] or part segmentation [27]). However, both methods have obvious weaknesses. Generally, the estimated poses from direct solutions are not so well-aligned with the images (Fig. 1(a)), because joint rotations are more difficult to regress compared with keypoints [19,36]. On the contrary, though indirect solutions tend to have better estimation precision, their performance heavily relies on the precision of the intermediate proxies and thus are vulnerable to noise and error in the predicted keypoints or part segmentation (Fig. 1(b)).


Figure 1. Comparisons of (a) the direct method [29], (b) the indirect method [36], and (c) our method.

To simultaneously achieve high precision and high robustness, some probabilistic methods are developed, which, instead of seeking a unique solution, try to explicitly model the uncertainty of human poses by learning some kind of probability distribution. Prevalent ways of modeling the distribution include multivariate Gaussian distributions [48, 56], normalizing flows [31], and neural networks [51, 53]. In practice, these learned probability distributions can notably improve the estimation results in some extreme cases (e.g., under large occlusion), however, only minor differences can be found in terms of the overall performances on large datasets. One reason is that these probability models cannot truly reflect the rotational uncertainty since they are not strictly constrained to $\mathcal{S O}(3)$. Recently, [55] proposes to adopt the matrix Fisher distribution over $\mathcal{S O}(3)$ [8, 25] to model the rotational uncertainty caused by depth ambiguity. However, even with this mathematically-correct formulation, the actual performance does not improve much either, because the parameters of the matrix Fisher distribution are not easy for deep neural networks to learn directly.

To address this problem, we propose a new learningfriendly and mathematically-correct formulation for learning probability distributions for human mesh recovery. Our formulation is derived based on the facts that, (i) the joint rotations follow the matrix Fisher distribution over $\mathcal{S O}(3)$,
(ii) the unit directions of bones follow the von Mises-Fisher distribution [44], (iii) the bone direction can be viewed as the observation of joint rotation (i.e., the latent variable). It can be proven that the probability distributions of joint rotations conditioned on bone directions still follow the matrix Fisher distribution, which allows us to regress the posterior probability distribution of the 3D joint rotations in a Bayesian manner, and more importantly, in an analytical form. Moreover, we mathematically prove that the posterior probability of human joint rotations is more concentrated than the prior probability. Our experimental results demonstrate that such a characteristic makes the posterior probability an easier form to learn (for neural networks) than its prior counterpart.

Apart from the theoretical contributions, we also propose a new human mesh recovery framework that can utilize the learned analytical posterior probability. We demonstrate that this framework successfully achieves high precision and high robustness at the same time, and outperforms existing SOTA baselines. Furthermore, our framework enables seamless integration with additional sensors that can yield directional/rotational observations (e.g., multi-view cameras, optical markers, IMUs) due to its Bayesian nature. Different from naive multi-sensor fusion algorithms (e.g., Kalman filter [21]) that typically perform fusion at the inference stage, our framework allows fusion in the training stage to learn the noise characteristics of sensors, and thus has the potential to produce better precision. We demonstrate that our fusion mechanism can achieve similar effects to fusing the latent features from multiple sensor input branches, but is much more flexible since it does not require modification of the main backbone.

The key contributions of this paper are thereby:

- We derive a novel analytical formulation for learning probability distributions for human joint rotations, and theoretically prove that such formulation allows the regression of posterior probability distribution in a Bayesian manner.
- We propose a new framework for human mesh recovery by leveraging the learned analytical posterior probability and show that this framework outperforms existing SOTA baselines.
- We introduce a novel and flexible multi-sensor fusion mechanism that allows fusing different observations in the training stage.


## 2. Related work

In this section, we discuss related studies on human mesh recovery, which can be achieved by optimization-based and learning-based methods. Leveraging the parametric human
model [41,54], optimization-based approaches [2,9, 15, 51] fit the parameters via iteration while learning-based approaches regress the parameters with neural networks. Our work follows the learning paradigm, therefore we here mainly review recent advances in learning-based methods.

Direct methods: Given images as input, this kind of approach directly regresses the model parameters with neural networks. Different representations of rotation [22, 34, 74], supervision schemes [20, 29, 37] as well as temporal context $[5,13,23,26]$ are explored to improve performance. However, the gap between the image space and the abstract parameter space of statistical models makes it difficult to generate well-aligned estimations.

Indirect methods: Instead of regressing rotation representations from RGB images directly, plenty of works introduce proper intermediate or proxy representations, such as segmentation [27, 49, 68], IUV maps [64, 69, 70], keypoints [ $6,14,36,52$ ] or surface landmarks [30, 32, 42], to guide the learning of neural networks efficiently. HybrIK [36] decomposes the 3D rotation into solvable swings from 3D keypoints and extra predicted twists. PARE [27] learns to predict attention masks which are fused with image feature maps to provide body part information. These solutions may achieve higher precision, but generating only deterministic results and ignoring the uncertainty of estimation make them sensitive to noisy or erroneous proxy predictions.

Probabilistic methods: To deal with the uncertainty from occlusions or depth ambiguities, several works manage to produce multiple hypotheses [1] or a probability distribution [53]. I2L-MeshNet [48] predicts lixel-based 1D heatmaps for each human mesh vertex for uncertainty modeling. Sengupta et al. [56] assume simple multivariate Gaussian distributions over the parameters of the human model. ProHMR [31] learns a distribution of plausible 3D poses represented by normalizing flows, which is more powerful and expressive than Gaussian distributions. Recently Sengupta et al. [55] further represent the essential distribution of human joint rotation over $\mathcal{S O}(3)$ by adopting the matrix Fisher distribution [25], which can provide quantified uncertainty estimation. Despite a better explanation for ambiguities, the parameters of the above distribution are not easy to learn, limiting their overall performance on complicated scenes.

Multi-sensor fusion: Recently an increasing number of approaches attempt to integrate extra observations from other sensors, such as IMUs [10,65,66] and muli-view cameras [7, 71, 73], to obtain more reliable estimations. One simple strategy is combining all observations properly with


Figure 2. Overview of our framework. Given an input image, the multi-branch network predicts the prior matrix Fisher parameters $\boldsymbol{F}$, the 3D keypoints $\boldsymbol{J}$, and the SMPL shape parameters $\boldsymbol{\beta}$, respectively. The bone direction $\boldsymbol{d}$ calculated from $\boldsymbol{J}$ serves as the likelihood conditioned on 3D rotation. The posterior probability can be obtained based on Bayesian rules (Fusion), which still follows the matrix Fisher distribution, but with different parameters and larger confidences. Observations from additional sensors can also be fused into the posterior probability in the same manner. The corresponding human mesh can then be recovered using the estimated rotation and shape.

Kalman filter [21], which can be treated as a baseline. Some works [ $43,62,63$ ] fit the human model to evidence including images and IMUs through joint optimization. Apart from these test-time fusion schemes, several approaches [ 10,61 ] incorporate the fusing process into training by concatenating the features from images and IMUs directly. GeoFuse [72] reinforces the image features guided by IMUs to infer the occluded joints. Our framework is also flexible to perform multi-sensor fusion and generates competitive results without specific modification to the backbone.

## 3. Methods

In this section, we first mathematically introduce the probability distributions for orientations regarding rotations and directions (Sec. 3.1). Then, we model the human joint rotation and bone direction with the corresponding distribution, and derive the analytical formulation of the posterior probability of joint rotation conditioned on the bone direction with crucial conclusions and discussion (Sec. 3.2). Finally, we describe the proposed framework (Sec. 3.3) and learning details (Sec. 3.4).

### 3.1. Orientation probability distribution

Before delving into human modeling, we investigate the orientation representation for general rigid entities. Suppose $\boldsymbol{X} \in \mathbb{R}^{n \times p}$ is the parametric representation of the entity orientation, each column of which depicts the direction of a basis. $\boldsymbol{X}$ is on the Stiefel manifold $\mathcal{V}(n, p)$ if $\boldsymbol{X}^{T} \boldsymbol{X}=\boldsymbol{I}_{p}$, and when $n=p$, it further belongs to the orthogonal group $\mathcal{O}(n)$. Additionally, the components of $\mathcal{O}(n)$ with determinant +1 are referred to as the special or-
thogonal group $\mathcal{S O}(n)$, which is used to represent the rotation of $n$ degrees of freedom. Meanwhile, if $p=1$, the normalized $\boldsymbol{X}$, i.e., $n$-dimensional unit vector on the manifold ( $n-1$ )-sphere $\mathcal{S}^{n-1}$, can represent the single direction as well. From a probabilistic perspective, when $\boldsymbol{X}$ is a random matrix, there are two common cases.

Rotation ( $n=p$ ): For rotation matrix $\boldsymbol{R} \in \mathcal{S O}(n)$, the matrix Fisher distribution $\mathcal{M F}(\cdot)$ has been proposed to characterize its probabilistic properties on $\mathcal{S O}(n)$ [8, 25]. The probability density function is as follows:

$$
\begin{equation*}
p(\boldsymbol{R} ; \boldsymbol{F})=\frac{1}{c(\boldsymbol{F})} \exp \left(\operatorname{tr}\left(\boldsymbol{F}^{T} \boldsymbol{R}\right)\right) \sim \mathcal{M} \mathcal{F}(\boldsymbol{F}), \tag{1}
\end{equation*}
$$

where $\boldsymbol{F} \in \mathbb{R}^{n \times n}$ is the distribution parameter, and $c(\boldsymbol{F})$ is a normalizing constant. Algebraically, $\boldsymbol{F}$ can be decomposed into a concentration matrix $\boldsymbol{K}$ and a mean rotation matrix $M$ via SVD decomposition:

$$
\begin{equation*}
\boldsymbol{F}=\boldsymbol{U} \boldsymbol{S} \boldsymbol{V}^{T}=\underbrace{\left(\boldsymbol{U} \Delta \boldsymbol{V}^{T}\right)}_{\boldsymbol{M} \in \mathbb{R}^{n \times p}} \underbrace{\left(\boldsymbol{V} \Delta \boldsymbol{S} \boldsymbol{V}^{T}\right)}_{\boldsymbol{K} \in \mathbb{R}^{p \times p}}, \tag{2}
\end{equation*}
$$

where $\Delta=\operatorname{diag}(1,1,|\boldsymbol{U} \boldsymbol{V}|)$ is a diagonal orthogonal matrix to ensure the determinant of $M$ is +1 . $\boldsymbol{K}$ is symmetric positive definite as long as $\boldsymbol{F}$ is full rank. A rotation estimation $\hat{\boldsymbol{R}}$ can be calculated from the mode of distribution:

$$
\begin{equation*}
\hat{\boldsymbol{R}}=\boldsymbol{M}=\boldsymbol{U} \operatorname{diag}(1,1,|\boldsymbol{U} \boldsymbol{V}|) \boldsymbol{V}^{T} \tag{3}
\end{equation*}
$$

Direction $(p=1)$ : The probability density function for a unit vector $\boldsymbol{d} \in \mathcal{S}^{n-1}$ is similar to Eq. (1) if we set $p=1$,
which corresponds to the classical von Mises-Fisher distribution $\mathcal{V} \mathcal{M} \mathcal{F}(\cdot)$ [44]:

$$
\begin{equation*}
p(\boldsymbol{d} ; \kappa, \boldsymbol{m})=\frac{1}{c(\kappa)} \exp \left(\kappa \boldsymbol{m}^{T} \boldsymbol{d}\right) \sim \mathcal{V} \mathcal{M} \mathcal{F}(\boldsymbol{m}, \kappa) \tag{4}
\end{equation*}
$$

where $c(\kappa)$ is a normalizing constant. $\boldsymbol{m}$ denotes the mean direction and $\kappa$ denotes the concentration parameter, which have a close meaning to $\boldsymbol{M}$ and $\boldsymbol{K}$ in Eq. (2), respectively, and thus $\hat{\boldsymbol{d}}=\boldsymbol{m}$ becomes a direction estimation.

Theoretically, if $\kappa$ is $0, \mathcal{V M \mathcal { F }}(\boldsymbol{m}, 0)$ is equivalent to the uniform distribution on the sphere, while if $\kappa$ is large, it is close to the wrapped normal distribution $\mathcal{W N}\left(\boldsymbol{m}, \kappa^{-1}\right)$ that adds up the densities of vectors representing the same direction on the sphere due to the periodicity. Thus, $\kappa$ can be viewed as the inverse of the variance and denotes the concentration of the distributions.

### 3.2. Human modeling

The human joint rotation can be represented as rotation matrix $\boldsymbol{R} \in \mathcal{S O}(3)$. Inspired by recent advances in object pose estimation [3, 33, 46, 67], we incorporate the probabilistic modeling for human poses. Specifically, we adopt the matrix Fisher distribution over $\mathcal{S O}(3)$ as the prior distribution for joint rotation. Moreover, as the bone direction can be easily calculated from the joint rotation, we regard the joint rotation $\boldsymbol{R}$ as the latent variable and the bone direction $\boldsymbol{d}$ as the corresponding observation, which follows the von Mises-Fisher distribution:

$$
\begin{equation*}
p(\boldsymbol{d} \mid \boldsymbol{R})=\frac{1}{c(\kappa)} \exp \left(\kappa \boldsymbol{l}^{T} \boldsymbol{R}^{T} \boldsymbol{d}\right) \sim \mathcal{V} \mathcal{M} \mathcal{F}(\boldsymbol{R} \boldsymbol{l}, \kappa) \tag{5}
\end{equation*}
$$

where $l$ is the unit direction of the bone in the reference pose (e.g., T-pose), ideally satisfying $\boldsymbol{R l}=\boldsymbol{d}$.

Leveraging Bayesian inference, given the prior distribution (Eq. (1)) and the likelihood function (Eq. (5)), the posterior probability of joint rotation conditioned on the bone direction can be derived as follows:

$$
\begin{align*}
& p(\boldsymbol{R} \mid \boldsymbol{d})=\frac{p(\boldsymbol{R}) \cdot p(\boldsymbol{d} \mid \boldsymbol{R})}{p(\boldsymbol{d})} \propto p(\boldsymbol{R}) \cdot p(\boldsymbol{d} \mid \boldsymbol{R})  \tag{6}\\
& \quad=\frac{1}{c} \exp \left(\operatorname{tr}\left[\left(\boldsymbol{F}+\kappa \boldsymbol{d} \boldsymbol{l}^{T}\right)^{T} \boldsymbol{R}\right]\right) \sim \mathcal{M} \mathcal{F}\left(\boldsymbol{F}+\kappa \boldsymbol{d} \boldsymbol{l}^{T}\right)
\end{align*}
$$

It can be concluded from Eq. (6) that the posterior probability $p(\boldsymbol{R} \mid \boldsymbol{d})$ also follows the matrix Fisher distribution with an updated parameter $\boldsymbol{F}^{\prime}=\boldsymbol{F}+\kappa \boldsymbol{d} \boldsymbol{l}^{T}$.

Property: From another perspective, the posterior parameter $\boldsymbol{F}^{\prime}$ can be viewed as the multiplication of the same mean term $\boldsymbol{M}$ and a new concentration term $\boldsymbol{K}^{\prime}$ :

$$
\begin{equation*}
\boldsymbol{F}^{\prime}=\boldsymbol{F}+\kappa \boldsymbol{d} \boldsymbol{l}^{T}=\boldsymbol{M}(\underbrace{\boldsymbol{K}+\kappa \boldsymbol{M}^{T} \boldsymbol{d} \boldsymbol{l}^{T}}_{\boldsymbol{K}^{\prime}}) . \tag{7}
\end{equation*}
$$

It can be proved that $\boldsymbol{M}^{T} \boldsymbol{d} \boldsymbol{l}^{T}=\boldsymbol{l} \boldsymbol{l}^{T}$ is a real symmetric matrix with rank 1, and $\boldsymbol{K}$ from Eq. (2) is also real symmetric, thus the posterior concentration term $\boldsymbol{K}^{\prime}$ is a real symmetric matrix. According to the interlacing theorem for Hermitian matrices from matrix analysis [17], the eigenvalues for a Hermitian matrix with a rank-1 Hermitian perturbation satisfy the following inequality:

$$
\begin{equation*}
\lambda_{1} \leq \lambda_{1}^{\prime} \leq \lambda_{2} \leq \cdots \leq \lambda_{p-1}^{\prime} \leq \lambda_{p} \leq \lambda_{p}^{\prime} \tag{8}
\end{equation*}
$$

where $\lambda_{i}$ and $\lambda_{i}^{\prime}$ denote the eigenvalues of $\boldsymbol{K}$ and $\boldsymbol{K}^{\prime}$, respectively. Note that the eigenvalues of the concentration term equal the singular values of the distribution parameter, which reflect the confidence of the distribution. From Eq. (8) we can get the conclusion that the posterior estimation is more concentrated than the prior estimation as long as the likelihood term is non-zero, and is validated to be a more easily learnable formulation in the experiment and the supplementary material.

General form: Similarly, if other sensors that yield directional $\boldsymbol{d}_{i}$ or rotational $\boldsymbol{D}_{j}$ observations are available, the analytical posterior probability is thereby as follows:

$$
\begin{equation*}
p\left(\boldsymbol{R} \mid\left\{\boldsymbol{d}_{i}, \boldsymbol{D}_{j}\right\}\right) \sim \mathcal{M} \mathcal{F}\left(\boldsymbol{F}+\sum_{i \in \mathcal{Z}_{1}} \kappa_{i} g\left(\boldsymbol{d}_{i}\right)+\sum_{j \in \mathcal{Z}_{3}} \boldsymbol{D}_{j} \boldsymbol{K}_{j}^{T}\right) \tag{9}
\end{equation*}
$$

where $\kappa_{i}$ and $\boldsymbol{K}_{j}$ are the concentration terms for weighting. $g(\cdot)$ is a mapping of IK that converts the directional observation to a rotation estimation, which is not limited to a specific IK algorithm as long as it supports gradient backpropagation (e.g., the simple solution $\boldsymbol{d l ^ { T }}$ in Eq. (6)). $\mathcal{Z}_{1}$ denotes the set of sensors providing directional observations such as accelerometers, while $\mathcal{Z}_{3}$ denotes the set of rotational sensors like gyroscopes. We simplify the original derivation by assuming the sensors are unbiased. Please refer to the supplementary material for the derivation.

Discussion: There are several advantages of our approach. First, adopting the matrix representation is more reasonable than other rotation representations. As presented in [34], a continuous 9D unconstrained representation followed by SVD can achieve comparable or even better performance than the widely used 6D vector [74]. Second, the Gaussian distribution is unsuitable for cases with large uncertainty where the assumption of local linearity cannot hold [11, 12], while the matrix Fisher distribution does not have this problem. Third, the posteriors are easier to learn than the priors in that learning the posteriors can converge to the mode preferred by the likelihood function quickly, while learning the priors may face multiple local minima in the initial stage and thus cannot converge well.

To recognize the proposed scheme intuitively, we show the schematic diagrams of probabilistic modeling in Fig. 3. For a method without probabilistic modeling (e.g., using IK


Figure 3. Schematic diagrams of probabilistic modeling. The opaque coordinate system $\lambda$ is the ground-truth 3D rotation. The transparent rotation represents a deterministic estimation for a method without probabilistic modeling (row 1), while it denotes a sample from the estimated posterior distribution (row 2). The red region on the sphere represents the probability of a certain rotation, and it could cover the ground-truth even for noisy cases.
to solve rotations from keypoints), its underlying model is a single direction, thus it may be erroneous when the estimated bone direction deviates from the ground-truth, as shown in the noisy cases. In contrast, the posterior model can be fused with various models, and for noisy keypoints, it has the potential to recover the exact rotations since the negative impact of its partial reliance on the estimated keypoints can be eliminated by the prior or other observations.

### 3.3. Learning Framework

Our proposed framework that leverages the derived posterior probability for human mesh recovery is demonstrated in Fig. 2. We adopt the parametric model SMPL [41] as our human representation, which can also be replaced by other human models [51,54]. Given an input image, a CNN backbone is used to extract image features, followed by three output branches, including prior distribution parameter $\boldsymbol{F}$, 3D keypoints $\boldsymbol{J}$, and shape parameter $\boldsymbol{\beta}$. The adopted keypoints branch consists of normalized 2D keypoints and relative depth to the root joint decoded from the feature, as well as the human scale predicted by a small MLP branch, so as to recover absolute 3D keypoints. Note that other strategies for 3D keypoints estimation are also applicable. The bone direction $\boldsymbol{d}$ is calculated from $\boldsymbol{J}$. Then we utilize Eq. (9) to fuse $\boldsymbol{F}, \boldsymbol{d}$, or other optional observations analytically in the sense of probability. With the new distribution parameter $\boldsymbol{F}^{\prime}$, we can get the rotation estimation according to Eq. (3). As for $\kappa$, it is related to the physical properties (measure covariance) of specific sensors that could be set in advance. If there is no prior knowledge of the sensor, it's feasible to tune it manually or learn it from the data. We simply use the scaled scores of estimated keypoints. For multiple sensors, the concentration term $\boldsymbol{K}$ is simplified as a diagonal matrix.

Objective functions: For the following objective functions, symbols with superscript '*' indicate the groundtruth, and symbols with hat indicate the estimation. The $L_{1}$ loss is used to supervise the 3D keypoints, while the $L_{2}$ loss is applied to other variables:

$$
\begin{align*}
& \mathcal{L}_{J}=\left\|\hat{\boldsymbol{J}}-\boldsymbol{J}^{*}\right\|_{1}  \tag{10}\\
& \mathcal{L}_{\beta}=\left\|\hat{\boldsymbol{\beta}}-\boldsymbol{\beta}^{*}\right\|_{2}^{2} \tag{11}
\end{align*}
$$

The mode of the posterior probability distribution $\hat{\boldsymbol{R}}$ can be solved according to Eq. (6) and (3), and is supervised if the annotations of SMPL pose parameters $\boldsymbol{\theta}$ are provided as follows:

$$
\begin{equation*}
\mathcal{L}_{\theta}=\left\|\hat{\boldsymbol{R}}-\operatorname{expm}\left(\boldsymbol{\theta}^{*}\right)\right\|_{2}^{2} \tag{12}
\end{equation*}
$$

where expm denotes the exponential map implemented with the Rodrigues' formula.

Apart from the mode, the whole distribution also needs to be supervised. Since the normalizing constant in the distribution is hard to be calculated stably due to the numerical integration, we propose to supervise the distribution by sampling. Specifically, we adopt the rejection sampling technique to sample Bingham distribution of unit quaternions on $\mathcal{S}^{3}$ based on its equivalence to matrix Fisher distribution. The proposal distribution in rejection sampling is angular central Gaussian (ACG) distribution [24, 55]. Thus the sampling loss is as follows:

$$
\begin{equation*}
\mathcal{L}_{s}=\sum_{i=1}^{N_{s}} \rho\left(\left\|\hat{\boldsymbol{R}}_{i}-\operatorname{expm}\left(\boldsymbol{\theta}^{*}\right)\right\|_{2}^{2}\right), \tag{13}
\end{equation*}
$$

where $N_{s}$ is the number of samples. $\rho$ is an simple activation function for relaxation, which tolerates small deviations.

The total objective function is as follows:

$$
\begin{equation*}
\mathcal{L}=w_{1} \mathcal{L}_{J}+w_{2} \mathcal{L}_{\beta}+w_{3} \mathcal{L}_{\theta}+w_{4} \mathcal{L}_{s} \tag{14}
\end{equation*}
$$

where $w_{1}, w_{2}, w_{3}$, and $w_{4}$ are weight scalars.

### 3.4. Implementation details

We adopt ResNet-34 [16] and HRNet-W48 [58] as backbones. The ResNet backbone is followed by three deconvolutional layers to generate 3D heatmaps with the size of $64 \times 64 \times 64$ for keypoints and three MLPs for shape parameters $\boldsymbol{\beta}$ (10), distribution parameter $\boldsymbol{F}$ (216) and human scale (1). The feature from HRNet backbone is upsampled and directly followed by similar output branches with dimensions motioned above. The input image has a resolution of $256 \times 256$. The network is trained for 50 epochs with Adam and an initial learning rate of $1 \times 10^{-3}$, decayed with a factor of $10 . w_{1}$ and $w_{2}$ are set to 1. $w_{3}$ and $w_{4}$ are set to 0.1 and increased to 1 in the later stage of training.

## 4. Experiments

In this section, we demonstrate the effectiveness of our framework on human mesh recovery and multi-sensor fusion, evaluate our key designs via an ablation study, and discuss the limitation and future work of our method.

### 4.1. Datasets and metrics

To maintain the fairness of comparison, we adopt the same datasets and metrics as previous methods.
Human3.6M [18] provides 3D keypoints annotations, and the corresponding SMPL annotations are from MoSh [40]. We use ( $\mathrm{S} 1, \mathrm{~S} 5, \mathrm{~S} 6, \mathrm{~S} 7, \mathrm{~S} 8$ ) for training and ( $\mathrm{S} 9, \mathrm{~S} 11$ ) for evaluation, following standard practice [22,36].
3DPW [62] provides SMPL annotations. Following [36, 37], we add its training set only for experiments on it.
MS COCO [39] contains in-the-wild images and 2D keypoints annotations. We use its training set to improve the generalization ability of our method.
MPI-INF-3DHP [45] is a multi-view dataset that provides 3D keypoints annotations. We only use it for training.
AGORA [50] is a synthetic dataset with challenging scenes and SMPL annotations of adults and kids. Only when evaluating our algorithm on it will we add its training set.
TotalCapture [61] contains multi-view videos, IMUs and 3D keypoints annotations for the evaluation of sensor fusion algorithms. We follow $[61,72]$ to divide it.
Metrics include MPJPE, PA-MPJPE, and PVE all in mm. MPJPE measures the 3D keypoints error, while PA-MPJPE is similar to MPJPE except that a rigid alignment is performed at first. PVE measures the human mesh vertex error.

### 4.2. Human mesh recovery

Table 1 shows the evaluation results on public benchmarks. With either ResNet or HRNet as the backbone, our approach outperforms SOTA methods. Besides, we surpass the prior counterpart [55] by a large margin, indicating that our posterior estimation is easier to learn than the single prior. Table 2 shows the results on the AGORA test set. Our framework is more accurate than others, especially for kids. Note that for 2D datasets, despite that the pseudo-GT annotator of CLIFF [37] and EFT dataset [20] can be incorporated to further improve our performance, we only use the original keypoints supervision for fair comparisons.

Posterior effects: We compare different designs to thoroughly validate the posterior effects and the feature choice in our framework, as shown in Table 3, which include: (a) regressing the parameters $\boldsymbol{F}$ only without the keypoint branch; (b) solving rotations from keypoints via IK without probabilistic modeling; (c) deactivating the learned prior parameters in testing (i.e., setting $\boldsymbol{F}$ to zero); (d) using the feature close to the end of the backbone to regress prior $\boldsymbol{F}$

| Methods | 3DPW |  |  | Human3.6M |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | PA $\downarrow$ | MPJPE $\downarrow$ | PVE $\downarrow$ | PA $\downarrow$ | MPJPE $\downarrow$ |
| HMR ( $R-50$ ) [22] | 81.3 | 130.0 | - | 56.8 | 88.0 |
| GraphCMR (R-50) [30] | 70.2 | - | - | 50.1 | - |
| SPIN (R-50) [29] | 59.2 | 96.9 | 116.4 | 41.1 | 62.5 |
| Sengupta. (H-48) [55]* | 59.2 | 84.7* | - | - | - |
| HMR-EFT ( $R-50$ ) [20] | 52.4 | - | - | 43.9 | - |
| I2L-MeshNet ( $R-50$ ) [48] | 58.6 | 93.2 | - | 41.7 | 55.7 |
| SPEC (R-50) [28] | 53.2 | 96.5 | 118.5 | - | - |
| BEV ( $H-32$ ) [60] | 46.9 | 78.5 | 92.3 | - | - |
| PARE (H-32) [27] | 46.5 | 74.5 | 88.6 | - | - |
| Graphormer (H-64) [38] | 45.6 | 74.7 | 87.7 | 34.5 | 51.2 |
| PyMAF (H-48) [70] | 45.3 | 74.2 | 87.0 | 37.2 | 54.2 |
| HybrIK (R-34) [36] | 45.0 | 74.1 | 86.5 | 33.6 | 55.4 |
| FastMETRO (R-50) [4] | 48.3 | 77.9 | 90.6 | 37.3 | 53.9 |
| FastMETRO (H-64) [4] | 44.6 | 73.5 | 84.1 | 33.7 | 52.2 |
| CLIFF (R-50) [37] | 45.7 | 72.0 | 85.3 | 35.1 | 50.5 |
| CLIFF (H-48) [37] | 43.0 | 69.0 | 81.2 | 32.7 | 47.1 |
| Ours (R-34) | 44.1 | 71.8 | 84.9 | 31.6 | 48.7 |
| Ours (H-48) | 40.6 | 68.3 | 79.4 | 29.1 | 45.7 |

Table 1. Results on standard benchmarks. 'PA' is PA-MPJPE. ' $R$ ' and ' $H$ ' mean ResNet and HRNet. * with scale correction.

| Methods | AGORA |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
|  | MPJPE $\downarrow$ | PVE $\downarrow$ | Kid-MPJPE $\downarrow$ | Kid-PVE $\downarrow$ |
| HMR [22] | 180.5 | 173.6 | 219.4 | 209.3 |
| HMR-EFT [20] | 165.4 | 159.0 | 202.7 | 193.5 |
| SPIN [29] | 153.4 | 148.9 | 191.7 | 186.7 |
| PARE [27] | 146.2 | 140.9 | 193.9 | 186.4 |
| SPEC [28] | 112.3 | 106.5 | 171.0 | 163.2 |
| ROMP [59] | 108.1 | 103.4 | 159.8 | 156.6 |
| BEV [60] | 105.3 | 100.7 | 129.1 | 125.9 |
| Hand4Whole [47] | 89.8 | 84.8 | 153.3 | 146.4 |
| CLIFF [37] | 81.0 | 76.0 | 94.1 | 89.6 |
| HybrIK [36] | 77.0 | 73.9 | 90.2 | 86.6 |
| Ours | $\mathbf{7 4 . 4}$ | $\mathbf{7 0 . 9}$ | $\mathbf{8 4 . 5}$ | $\mathbf{8 0 . 5}$ |
| PLIKS [57] | 71.5 | 67.3 | 88.3 | 84.2 |
| NIKI [35] | 67.3 | 63.9 | 83.9 | 80.2 |

Table 2. Results on the AGORA test set. The metrics with the prefix 'Kid-' are calculated only for kids, otherwise for all ages. Two concurrent works are shown in gray for completeness.

| Designs | Human3.6M |  |
| :--- | :---: | :---: |
|  | PA-MPJPE $\downarrow$ | MPJPE $\downarrow$ |
| (a) W/o 3D keypoints | 45.8 | 76.5 |
| (b) W/o prior $\boldsymbol{F}$ | 43.2 | 63.6 |
| (c) W/o prior $\boldsymbol{F}$ (in testing) | 42.7 | 58.7 |
| (d) Late feature for $\boldsymbol{F}$ and $\boldsymbol{\beta}$ | 29.9 | 48.6 |
| (e) Early feature for $\boldsymbol{F}$ and $\boldsymbol{\beta}$ | 29.3 | 46.5 |
| (f) Ours (full model) | $\mathbf{2 9 . 1}$ | $\mathbf{4 5 . 7}$ |

Table 3. Ablation study of designs on the Human3.6M dataset.
and shape $\boldsymbol{\beta}$; (e) using the feature from the initial stage; (f) our full model with all branches and intermediate feature.

The performance of design (a) is not good since its estimation cannot align precisely with the image, and it is observed that this design exhibits a slower speed of convergence, reflecting the importance of the likelihood function


Figure 4. Noise simulation. (a) Rotation error v.s. the mixed noises of both prior and keypoint. (b) Rotation/direction error v.s. keypoint noise. The noise level is the ratio of the noise amplitude to the maximum of the variable. The simulation step is $5 \%$. 'W/o prior $\boldsymbol{F}$ ' is an indirect strategy without probability. 'Fixed $\kappa$ ' uses predefined $\kappa$. 'Adaptive $\kappa$ ' means $\kappa$ varies with the noise variance.

| Noise amplitude | 5 mm | 10 mm | 15 mm | 30 mm | 50 mm |
| :--- | :---: | :---: | :---: | :---: | :---: |
| W/o prior $\boldsymbol{F}$ | 61.3 | 62.7 | 65.0 | 71.5 | 80.4 |
| Posterior-based | 48.5 | 49.6 | 51.4 | 54.5 | 59.0 |
|  | $(12.8 \downarrow)$ | $(13.1 \downarrow)$ | $(13.6 \downarrow)$ | $(17.0 \downarrow)$ | $(21.4 \downarrow)$ |

Table 4. Noise test on the Human3.6M dataset. The 3D keypoints suffer from different levels of noises. MPJPE is reported.
from keypoints. The comparison between design (b) and (e) shows that the prior $\boldsymbol{F}$ is crucial in fusion. Furthermore, design (c) is better than design (b), indicating the prior $\boldsymbol{F}$ has guided the keypoints learning to some extent. The difference is more significant in MPJPE since the global rotation is supervised for design (c). As for the feature choice, the intermediate feature adopted by our framework shows slightly better performance than the late and early features.

Noise robustness: We evaluate the robustness of our framework when suffering from noise. Fig. 4 shows the simulation results with two metrics. The rotation error is the angle to be rotated from the estimated rotation $\hat{\boldsymbol{R}}$ to the ground-truth. The direction error is the angle between the estimated bone vector and the ground-truth. Fig. 4 (b) reveals that 'w/o prior $\boldsymbol{F}$ ' has a small direction error but a large rotation error for the unsolved twist, while the posterior strategy has a much smaller error even with a high keypoint noise level and shows a slower error growth rate. Note that the performance of a simple fixed $\kappa$ is also acceptable. Fig. 4 (a) shows that when the prior noise level is less than $15 \%$, the keypoint noise has little effect on the posterior result with the adaptive $\kappa$, reflecting the tolerance to noises of the posterior scheme. Table 4 shows the noise test on the Human3.6M dataset. From the difference listed in parentheses, when the noise level is higher, the error of the posterior method increases more slowly compared with the baseline without prior $\boldsymbol{F}$.

Samples illustration: Fig. 5 illustrates the samples from the posterior distribution. The right hand has a relatively


Figure 5. Samples from the distribution. The mode and samples of the relative rotations are shown. The light color indicates the mode, while the dark color indicates an extra sample. The canonical coordinate is at the top right as a reference.

| Methods | Sensors | TotalCapture |  |
| :--- | :---: | :---: | :---: |
|  |  | PA-MPJPE $\downarrow$ | MPJPE $\downarrow$ |
| IMUPVH [10] | mv + IMUs | - | 42.6 |
| GeoFuse [72] | mv + IMUs | 20.6 | 24.6 |
| Ours | mv + IMUs | $\mathbf{1 9 . 4}$ | $\mathbf{2 3 . 5}$ |
| VIP [62] | sv + IMUs | 26.0 | - |
| Kalman filter | sv + IMUs | 23.1 | 34.7 |
| Ours | sv | 29.0 | 42.1 |
| Ours (w/o ref, $R-50)$ | sv + IMUs | 25.8 | 41.7 |
| Ours (w/o ref, $H-48)$ | sv + IMUs | 22.3 | 38.8 |
| Ours $(R-50)$ | sv + IMUs | 25.0 | 32.3 |
| Ours $(H-48)$ | sv + IMUs | $\mathbf{2 1 . 2}$ | $\mathbf{2 8 . 5}$ |

Table 5. Results on the TotalCapture dataset. 'mv' and 'sv' denote multi-view and single-view. 'w/o ref' means lacking a reference skeleton (only a statistical one from training set is adopted), which would slightly weaken the performance of our framework.
large uncertainty on rotating around the X -axis due to the uncertain twist angle, as shown by the widespread blue and green samples. The left elbow has a vertical uncertainty on the direction of the forearm since the left hand cannot be easily determined. The left ankle has large confidence, except in the depth direction, therefore the green samples spread horizontally.

Fig. 6 shows the qualitative comparison with the SOTA methods. The indirect methods that use part segmentation [27] or 3D keypoints [36] perform well in most cases, but may suffer from wrong segmentation for distant people or generate unnatural poses. While the direct method CLIFF [37] may not align the image well for complicated scenes.

### 4.3. Multi-sensor fusion

We perform experiments on the TotalCapture dataset [61] using the feed-forward network directly without any iterative optimization. As the original dataset does not provide SMPL annotations, we adopt the human skeleton defined by 19 joints and 11 attached IMUs, as shown in Fig. 7. We choose the optimization-based method VIP [62] and the feature-fused method GeoFuse [72] as baselines.


Figure 6. Qualitative comparison. The input images are from 3DPW [62], MS COCO [39], and AGORA [50], respectively. We compare our approach with SOTA methods including HybrIK [36], PARE [27], and CLIFF [37]. For images with multiple people, the person with a solid yellow circle on the face is estimated.


Figure 7. An example of a multi-sensor case. The estimations from the front-view camera, side-view camera, and IMUs are plotted. The normalized confidence score of the left knee is listed.

Table 5 shows the experimental results. Our method outperforms baseline methods, indicating the effectiveness of our posterior scheme. In the 'Kalman filter' setup, we apply a weighted sum to the 3D rotations separately obtained from images and IMUs. As the observation variance required for calculating the Kalman gain is unknown, we pick the weight pairs that can yield the best estimation through grid searching, i.e., from $(0.7,0.3)$ to $(0.3,0.7)$. Note that unlike Kalman filter which fuses the observations in the testing stage, our method performs fusing in the training stage, and thus has the potential to obtain higher precision. Our framework is also more flexible than feature-level fusing methods since we do not require modifications of the backbone to incorporate new sensors.

Fig. 7 shows an example of a scene with multiple cameras and IMUs. The confidences from the two cameras are
calculated via the normalized differential entropy of the estimated distribution parameters, while the confidence from IMUs is set to a relatively larger value since IMUs can provide accurate measurements. Note that other metrics that represent the uncertainty from the distribution can also be adopted. It can be observed that the front view produces erroneous knee bending due to the depth ambiguity, therefore its confidence is lower than the side view. As a result, the fused result will be less affected by the noisy estimation.

### 4.4. Limitation and future work

Our work has several limitations. First, we only consider the uncertainty of poses, not including that of shapes, which can also be modeled as probability distributions. Second, we model the human joint independently, which is only affected by the parent node. Therefore, how to derive the analytical form of joint rotations conditioned on other hierarchical joints to incorporate anatomical constraints explicitly is still unsolved. Besides, with the single-view uncertainty, the temporal extension also deserves further investigation.

## 5. Conclusion

In this paper, we derive a novel analytical posterior probability for human joint rotations in a Bayesian manner and prove the property that the posteriors are more concentrated than the priors. Based on the derivation, we propose a new framework for human mesh recovery by leveraging the learned posteriors, which has high precision and robustness, outperforming existing SOTA baselines. Furthermore, our framework can be seamlessly incorporated with additional sensors in the training due to its Bayesian nature. Our research also provides a sound foundation for incorporating more advanced prior conditions or physical constraints.

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